Introduction to Inductive Logic Programming

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About me

- n assistant at ICS, UPJŠ in Košice
- n PhD. student of prof. Peter Vojtáš, Prague
- n research interests concerns ILP
 - •• ordinal classification
 - ^{••} fuzzy ILP
 - Generalized Annotated Programs induction
 - user preferences, profiles

The presentation

n Inductive Logic Programming (ILP)

- (Multi) Relational Data Mining method
- Machine Learning + Logic Programming
- ·· complex data structures
 - n medicine, genetics, chemistry, economic ...
- n Goals
 - " give basic knowledge on ILP
 - describe our results in this field

Outlines

n Basic concepts

n ILP techniques

- refinement graphs (FOIL)
- inverse resolution (CIGOL)
- relative least generalization (GOLEM)
- inverse entailment (ALEPH)
- n Applications
- n Future directions of ILP
- n Our research

Several forms of reasoning

- n (Background) Knowledge
 - Socrates is a human
- n Observations (Examples)
 - Socrates is mortal
- n Theory (Hypothesis)
 - " IF X is a human THEN X is mortal

Several forms of reasoning



Several forms of reasoning

n Deduction (Abduction)

- if the theory and background knowledge (examples) are true then the examples (background knowledge) are also true.
- n Induction
 - an induced theory from given examples and background knowledge need not be true in case of other examples or background knowledge not used in the induction process

General ILP task

n Given

- Background Knowledge B
- Examples *E*
 - n Positive e+
 - n Negative e⁻ (sometimes not used in the learning process)

n Find

- Hypothesis H, such that
 - n covers all positive examples (completeness)
 - n covers non of the negative examples (*consistency*)
 - n a complete and consistent hypothesis is correct

Normal setting (predictive)

n Representations

- example e <u>definite clause</u> (fact)
- background knowledge B definite program
- ·· hypothesis H definite program

n H *covers* e w.r.t. B if (*HÈB*) |= e

Normal setting (predictive)

n Positive examples

- { daughter(mary,ann), daughter(eve,tom) }
- n Negative examples
 - { daughter(tom,ann), daughter(eve,ann) }
- n Background Knowledge
 - { mother(ann,mary), mother(ann,tom), father(tom,eve), father(tom,ian), female(ann), female(mary), female(eve), male(ian), male(tom), parent(X,Y)←mother(X,Y), parent(X,Y) ← father(X,Y) }
- n Hypotheses
 - ^{...} { daughter(X,Y) ← female(X), parent(Y,X) }
 - { daughter(X,Y)←female(X), mother(Y,X); daughter(X,Y)←female(X), father(Y,X) }

n Representations

- example e <u>Herbrand interpretation</u>
 n often just positive examples
- background knowledge B definite program
- \cdots hypothesis *H* definite program

n H covers e w.r.t. B if

H is true in the least Herbrand model M(BÈE)

n Examples

- { mother(lieve,soetkin), father(luc,soetkin), parent(lieve,soetkin), parent(luc,soetkin), male(luc), female(lieve), female(soetkin), human(lieve), human(luc), human(soetkin) }
- { mother(blaguna,sonja), father(veljo,saso), father(veljo,sonja), parent(blaguna,saso), parent(blaguna,sonja), parent(veljo,saso), parent(veljo,sonja), male(veljo), male(saso), female(blaguna), female(sonja), human(veljo), human(saso), human(blaguna), human(sonja) }
- n Empty background knowledge
- n Hypothesis
 - { parent(X,Y)←mother(X,Y); parent(X,Y)←father(X,Y); mother(X,Y)√father(X,Y)←parent(X,Y); ←mother(X,Y),father(X,Y); human(X)←female(X); human(X)←male(X); female(X)√male(X)←human(X); ←female(X),male(X); female(X)←mother(X,Y); male(X)←father(X,Y); human(X)←parent(X,Y); human(Y)←parent(X,Y); ←parent(X,X) }

n Examples

- ~ { class(fix), worn(gear), worn(chain) }
- ** { class(sendback), worn(engine), worn(chain) }
- ** { class(sendback) ,worn(wheel) }
- `` { class(ok) }
- n Background knowledge
 - ~ { replaceable(gear), replaceable(chain), not_replaceable(engine), not_replaceable(wheel) }
- n Hypothesis

n Positive examples

- { daughter(mary,ann), daughter(eve,tom) }
- n Negative examples
 - { daughter(tom,ann), daughter(eve,ann) }
- n Background Knowledge
 - { mother(ann,mary), mother(ann,tom), father(tom,eve), father(tom,ian), female(ann), female(mary), female(eve), male(ian), male(tom), parent(X,Y)←mother(X,Y), parent(X,Y) ← father(X,Y) }
- n Hypotheses
 - $(aughter(X,Y) \leftarrow female(X), parent(Y,X) \}$
 - { ←daughter(X,Y), mother(X,Y); female(X)←daughter(X,Y); mother(X,Y)∨father(X,Y)←parent(X,Y) }

Predictive vs. Descriptive ILP

n Predictive

- Learn a reason why positives are positives and negatives are negatives
- You know what You are looking for, but you don't know what it looks like.
- Separate examples and background knowledge
- often used

n Descriptive

- Find something interesting about the data
- You don't know what You are looking for
- all background knowledge about an example is incorporated in this example

Completeness and Consistency









Specialisation vs. Generalization

- n C |= D
 - D is a specialisation of C
 - ··· C is a generalization of D

n if C $|\neq$ e then D $|\neq$ e n if D |= e then C |= e

The general ILP algorithm

n Input: E⁺, E⁻, B n Output: H

n begin

- initialize H
- ·· repeat
 - n if H is not consistent specialize it
 - n if H is not complete generalize it
- " until H is not correct
- ·· output H
- n end

Subsumption Theorem

- n cover relation "/="
 - hard to implement
 - not decidable
 - need a framework to solve this problem
- n subsumption
 - a clause C subsumes a clause D (C³D) if (\$q) Cq \hat{I} D n C=p(X) \leftarrow q(a),r(Y) = {p(X), \neg q(a), \neg r(Y)} ≥ {p(b), \neg q(a), \neg r(c), \neg s(Z)} = p(b) \leftarrow q(a),r(c),s(Z)=D for θ ={ X/b, Y/c}
 - if C ≥ D then C |= D (the converse does not hold) n C=P(f(X))←P(X), D=P(f²(X))←P(X)

Subsumption Theorem

- n SLD-refutation theorem
 - Let Σ is a set of Horn clauses. Then Σ is unsatisfiable iff $\Sigma \mid_{sr} \Box$.
- n SLD-Subsumption theorem
 - Let Σ is a set of Horn clauses and C a Horn clause. Then $\Sigma \models C$ iff $\Sigma \models_{sd} C$.
- n SLD-refutation theorem and SLD-Subsumption theorem are equivalent.
- **n** Σ |- _{sr} **C** if there exists an SLD-resolution of **C** from Σ .
- n $\Sigma \mid_{sd} C$ if there exists an SLD-resolution of a clause D from Σ such that D \geq C (D subsumes C)

Hypothesis space

- n Space of (all) Horn clauses H
 - ordered by subsumption
- **n** for every finite set $S \subseteq H$ there exists a greatest specialisation of S in H
- **n** for every finite set $S \subseteq H$ there exists a least generalisation of S in H
- **n** H ordered by \geq is a lattice
 - \perp bottom element
 - T top element



Hypothesis space

n Large space of all hypotheses

- need for a space of acceptable hypotheses
 - n language bias
- **n** Refinement operator $r:H \rightarrow H$
 - determine the hypothesis space (refinement graph)
 - specialisation operator
 - n $r(C)=D, C \models D$
 - applies a substitution θ to C
 - adds literal to the body of C
 - generalisation operator

n $r(C)=D, D \models C$

- applies an inverse substitution θ^{-1} to C
- removes literal from the body of C

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Searching refinement graphs

- n top-down searching of refinement graph n starting with $T = \Box$
- n depth-first search
- n implemented in system FOIL

Searching refinement graphs



Inverse resolution

- n bottom-up approach
- n applying inverse resolution to clauses
 - V-operators
 - n absorption
 - n identification
 - W-operators
 - n intra-construction
 - n inter-construction
- n predicate invention
- n not deterministic
- n implemented in system CIGOL

Inverse resolution

absorption



intra-construction







Inverse resolution



Relative least generalization

n H ∪ B |= e

- n Let H consist of single clause C
 n C \cup B |= e \Rightarrow C |= B \rightarrow e
 n if e atom, B atoms then e \leftarrow B is a Horn clause
- n C≥_BD if C≥(D∪{¬L₁, ..., ¬L_n}) n LGS((D₁∪{¬L₁, ..., ¬L_n}), ..., (D_m∪{¬L₁, ..., ¬L_n}) is an RLGS_B of {D₁, ..., D_m} relative to B={L₁, ..., L_n} in H
- n bottom-up approach
- searches correct LGRS_B of positive examples
 n implemented in system GOLEM

Relative least generalization

- n RLGS_B(daughter(mary,ann),daughter(eve,tom)) for B={female(mary), parent(ann,mary), female(eve), parent(tom,eve), female(ann)} is
- n daughter($V_{m,e}, V_{a,t}$) \leftarrow parent(ann,mary), parent(tom,eve), female(mary), female(eve), female(ann),parent($V_{a,t}, V_{m,e}$), female($V_{m,e}$), female($V_{m,e}$), female($V_{m,e}$), female($V_{m,e}$).
 - if C\{L} covers at least as many positive examples and at most as many negative examples as C then the literal L is irrelevant
- n after removing irrelevant literals we get daughter($V_{m,e}, V_{a,t}$) \leftarrow parent($V_{a,t}, V_{m,e}$), female($V_{m,e}$), so daughter(X,Y) \leftarrow parent(Y,X), female(X)

Inverse entailment

n H∪B |= e

- n Let H consist of single clause C
- n $C \cup B \models e \Rightarrow B \cup \neg e \models \neg C$
- n $\neg \bot$ is a (possibly infinite) conjunction of ground literals which are true in every model of B \cup $\neg e$
- n $\mathsf{B} \cup \neg \mathsf{e} \models \neg \bot$
- ${\tt n} \ \neg C$ is true in all models of $B \cup \neg e \Rightarrow \neg C$ contains a subset of $\neg \bot$
- n B $\cup \neg e \models \neg \bot \models \neg C \Rightarrow C \models \bot$

n top-down approach

- searches for clauses which subsumes \perp
- ability to have rules in background knowledge
- n implemented in system ALEPH
 - Ianguage declarations

Inverse entailment

- **n** $\perp_{daughter(mary,ann)} = daughter(A, B) :- mother(B, A), female(B), female(A), parent(B, A).$
- $n \perp_{daughter(eve,tom)} = daughter(A, B) :- father(B, A), female(A), male(B), parent(B, A).$
- $n H = \{ daughter(A, B) :- female(A), parent(B, A). \}$

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East-West trains

n what makes a train to go eastward?



Biology, Chemistry, ...

n what makes a molecule to be mutagenetic?





Other applications

n Engineering

- finite element mesh design
- detecting a traffic problem
- n Natural language processing
 - Iearning language grammars
 - speech tagging
 - text categorisation
- n Life Sciences
 - ^{...} 3D protein structure
 - predicting carcinogenicity

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Imperfection, imprecision

n Bayesian nets

n Probabilistic reasoning

n Fuzzy logic

Large data sets

n use of a power of databases
n distributed mining
n efficient choice of training set

Semantic web

n XML, ... n description logic, RDF

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Inductive Generalized Annotated Programming

- $\mathbf{n} \ A: \rho(\mu_1, \ \dots, \ \mu_k) \leftarrow B_1: \mu_1 \ \& \ \dots \ \& \ B_k: \mu_k$
- n the first approach to induce GAP programs
- n convenient for ordinal classification problems
- n equivalent to fuzzy logic programs
- n better representation of the real-world as probabilistic ILP approaches
- n multiple use of classical ILP system ALEPH with orderings in the background knowledge
- n succesfully used in a Slovak project NAZOU
 - learning user preferences

Inductive Generalized Annotated Programming



Inductive Generalized Annotated Programming

Hotel name	Location	Price (\$)
africa	centre	20
america	east	50
antarctica	west	80
australia	east	110
asia	west	50
europe	centre	80

Conference name	Location
icml	centre
ecml	East
ilp	West

Price (\$)	TV of "cheap"
20	1.0
50	0.7
80	0.4
110	0.1

TV of "near"				
from / to	centre	east	t wes	st
centre	1.0	0.7	0.4	
east	0.7	1.0	0.1	
west	0.4	0.1	1.0	
		-		
TV of "approppriateness of				
a hotel for a conference"			icml	ecml
		frica	1.0	1.0

i v or "approppriateness or	1		
a hotel for a conference"	icml	ecml	ilp
africa	1.0	1.0	0.7
america	1.0	1.0	0.1
antarctica	0.4	0.1	0.4
australia	0.1	0.1	0.1
asia	0.7	0.1	1.0
europe	0.4	0.4	0.4

Results of our algorithm:

A Hotel is appropriate for Conference with truth value at least 1 **IF** its price is cheap with truth value at least 0.7 **and** is located near the conference with truth value at least 0.7

A Hotel is appropriate for Conference with truth value at least 0.7 **IF** its price is cheap with truth value at least 0.7 **and** is located near the conference with truth value at least 0.4

A Hotel is appropriate for Conference with truth value at least 0.4 **IF** its price is cheap with truth value at least 0.4 **and** is located near the conference with truth value at least 0.4

Every Hotel is appropriate for Conference with truth value at least 0.1.

attribute values ordering

cheap(A,X) := le(X,Y), cheap(A,Y).near(A,B,X) := le(X,Y), near(A,B,Y).

le(0.1,0.4). *le*(0.4,0.7). *le*(0.7,1.0).

References

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